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**Flowerfree Finding of Maximum Matchings**

**Günther Stiege**

**Bericht**



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**Flowerfree Finding of Maximum Matchings**

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**Bericht**

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*Bibliographische Angaben:*

Stiege, Günther:  
Flowerfree Finding of Maximum Matchings / Stiege, Günther – Oldenburg: Universität  
Oldenburg, 2012  
(Berichte aus dem Department für Informatik Nr. 2/12)

ISSN 0946-2910

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# Flowerfree Finding of Maximum Matchings

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(June 2012)

**Abstract.** Actual algorithms for finding maximum matchings are based on Edmonds' techniques of shrinking and expanding circuits of odd length (blossoms and flowers). Here a new approach based on a modified alternating depth-first search is presented. It uses coupled recursion.

**Kurzfassung.** Derzeitige Algorithmen zum Finden maximaler Korrespondenzen basieren auf Edmonds' Techniken zum Schrumpfen und Expandieren von Kreisen ungerader Länge (Blüten und Blumen). Hier wird eine neue Lösung mit einer modifizierten alternierenden Tiefensuche vorgestellt. Sie benutzt gekoppelte Rekursion.

**Categories and Subject Descriptors:** E.1 [Data Structures] (Graphs and Networks).

**General Terms:** Algorithms

**Additional Keywords and Phrases:** maximum matching

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## 1 Introduction

The problem of finding a maximum matching in general graphs is important, interesting, and much discussed. It is central to discrete mathematics and algorithmic graph theory. In 1965 Edmonds [Edmo1965] published an algorithm to find such matchings. Although several improvements on the efficiency have been made since, Edmonds' main ideas still constitute the core of every algorithm for finding maximum matchings. To overcome the difficulties of odd length paths, Edmonds shrunk these paths to single entities (blossoms) which afterwards were expanded again (flowers). All actual algorithms for finding maximum matchings use the technique of shrinking and expanding.

Here a new solution is proposed. The main idea is: If vertex  $u$  can be reached from vertex  $v$  in an even number of steps and a first attempt yields an odd number of steps then there must be another path from  $v$  to  $u$  with an even number of steps. The problem is to find it with sufficient efficiency. The solution lies in allowing to traverse each line twice, once in each direction.

This report is organized as follows:

Section 2 summarizes the prerequisites. These are at the one hand results on augmenting paths. On the other hand, some implementation details of storing and traversing graphs are described.

Section 3 presents a motivating example.

In section 4 the algorithm is presented. It is proved that it does what it is supposed to do. Some remarks on its complexity conclude the section.

## 2 Prerequisites

### 2.1 Augmenting Paths

We assume simple graphs, i. e. undirected graphs without loops and without multiple edges. A path in a graph is a sequence of vertices where each vertex is joined to the next by an edge. The corresponding sequence of edges defines the path as well. A path is open if the first vertex differs from the last. A path is simple if no vertex occurs more than once. A matching is a set of mutually non-adjacent edges. A matching is saturated if no addition of an edge yields a greater matching. A matching is maximum if no other matching has a greater cardinality. Not every saturated matching is maximum. We will speak of *matching edges* and *non-matching edges*.

The central tool for finding maximum matchings are augmenting paths. A path is an *alternating path* if it is open and simple and if a matching edge is always followed by a non-matching edge and vice-versa. An *augmenting path* is an alternating path whose first edge and last edge are non-matching edges. As easily can be seen, changing matching edges to non-matching edges and vice-versa along the path yields a new matching with one more edge. The existence of an augmenting path is sufficient to make a matching larger. A famous theorem due to Berge [Berg1957a] and known as Berge's lemma states that the existence of an augmenting path is also a necessary condition for a matching not to be maximum.

A vertex is *exposed* with respect to a matching if none of its edges is a matching edge. The vertex is *covered* with respect to the matching if it is incident with a matching edge. The first vertex as well as the last vertex of an augmenting path are exposed vertices. If an exposed vertex is such, that no augmenting path starting in it can be found, then no posterior augmenting path will pass through that vertex. The vertex is classified as *frustrated* and need not be considered in the sequel.

## 2.2 Data Structures

We assume the graph represented by an incidence list structure. There are a list of vertices and a list of edges. Vertices as well as edges have identifying names. The graph structure is given by an incidence list adjoint to each vertex. For the matching algorithm described in the following section it is convenient to store some information in the vertex records and in the edge records. We have three fields (`vtattr`, `vtype` and `vactive`) for each vertex and one field (`edtype`) for each edge.

<code>vtype</code>	E C F	exposed covered frustrated
<code>vtattr</code>	U E O EO	unvisited even visit only odd visit only even visit as well as odd visit
<code>vactive</code>	FALSE TRUE	vertex not active vertex active
<code>edtype</code>	FALSE TRUE	non-matching line matching line

Table 1: *Data fields for algorithm FFMAT*

## 3 A Motivating Example

Figure 1 shows a graph in which we want to find an augmenting path. We have found

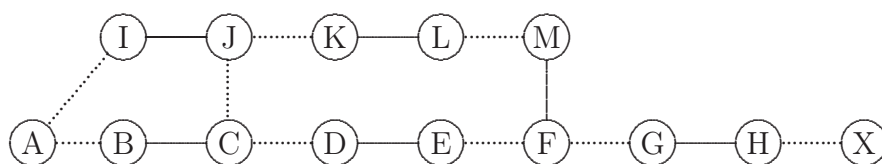


Figure 1: *Graph matchgraph*

already a matching in the graph. Solid lines indicate matching edges. Non-matching

edges are characterized by dotted lines. There are two exposed vertices in the graph, namely **A** and **X**. We want to find an augmenting path from **A** to **X**. To this end, we start an alternating depth-first search in **A**. There are several different runs of such a search. In our example, the choice of the first edge traversed is critical. In table 2 we see what

Depth-first search starting with edge AC								
AB	BC	CJ	JI	IA				
		CD	DE	EF	FM	ML	LK	KJ
AI								
Depth-first search starting with edge AI								
AI	IJ	JC	CB	BA				
		JK	KL	LM	MF	FE	ED	DC
						FG	GH	HX!

Table 2: *Different runs of an alternating depth-first search*

happens. In the upper part the dfs starts with edge **AB**, in the lower part it starts with edge **AI**.

*Upper part.* The first branch stops with edge **IA** since vertex **A** is still active. The second branch stops with edge **KJ** because vertex **J** had been visited before. The third and last branch stops immediately with edge **AI** since vertex **I** has also been visited previously. No augmenting path has been found.

*Lower part.* The first branch stops with line **BA** since vertex **A** is active. The second branch stops with edge **DC** because vertex **C** has been visited before. Finally, the last branch reaches vertex **X** along edge **HX**. An augmenting path has been detected and the procedure stops.

What now? The solution lies in differentiating the two cases where a branch is stopped. The first case occurs when the next vertex to be visited by the depth-first search is still active. This occurs along a “backward arc” and closes a circuit. No circuit can ever be part of an augmenting path and therefore the depth-first search always has to return. However, as can be seen in table 2 the depth-first search also returns at vertices which are not active anymore. They have been visited before and are visited again along so called “forward arcs“. These do not close circuits and there is no reason which forces stopping the search. A closer look at this case reveals that there are two kinds of visits to a vertex: *even visits* when the vertex is reached after an even number of steps and *odd visits* when the vertex is reached after an odd number of steps.

We now modify the alternating depth-first search in the following way. We allow an even visit to a vertex if it is as yet unvisited or if it had only an odd visit. We allow an odd visit in the corresponding situation. We do not allow multiple visits of the same kind because nothing new happens after such a visit. To illustrate the modified dfs we use again the graph of figure 1. Table 3 shows a run of the modified alternating depth-first search. An entry like **BC** followed by an entry *e* means that line **BC** is traversed and an even visit to **C** is made. In the table again we see two depth-first search trees. The first



Depth-first search with visit marking $e$ and $o$																
AB	$o$	BC	$e$	CJ	$o$	JI	$e$	IA	$o$	FM	$e$	ML	$o$	LK	$e$	KJ
AI	$o$	IJ	$e$	JC	$o$	CB	$e$	BA	$o$	MF	$e$	FE	$o$	ED	$e$	DC
				JK	$o$	KL	$e$	LM	$o$			FG	$o$	GH	$e$	HX!

Table 3: *Run of a modified alternating depth-first search*

starts with edge AB and the second with edge AI. The first tree has two branches. The first branch ends with edge IA since A is active. The second branch ends with edge KJ for J though actually inactive had a previous odd visit. The tree starting with edge AI is traversed next. The first branch traverses vertices which all have been visited already but with opposite even/odd characteristics and stops with active vertex A. The second branch passing again through a number of vertices with opposite even/odd marking eventually stops at vertex C who had previously visits of both kinds. Finally, the last branch passes through some vertices already visited and three unvisited vertices until reaching vertex X. An augmenting path has been found!.

## 4 Algorithm FFMAXMAT

### 4.1 Description of the Algorithm

In the following algorithm FFMAXMAT<sup>1</sup> is presented. The algorithm uses the modified alternating depth-first search approach. It consists of a main program FFMAXMAT and two recursively coupled routines, `evenvisit` and `oddvisit`. The programs are shown in tables 4, 5 and 6. They are formulated in a C-like pseudocode.

At the beginning all vertices are exposed and all edges are non-matching.

**FFMAXMAT:** This is the main loop. In it the list of all vertices is processed. For each vertex the indicators `vtattr` and `vtactive` of all vertices are reset (statement 3). Then it is checked whether the actual vertex is exposed and whether there is at least one other exposed vertex (statement 4). If so, then an alternating depth-first search is started in that vertex. This is done by calling the routine `evenvisit` (statement 5). In a coupled recursion routines `evenvisit` and `oddvisit` perform the modified alternating depth-first search and return eventually with an augmenting path or with the notification that there is none.

**evenvisit:** It expects a vertex and an edge as input parameters. The vertex is the vertex visited. The line, called *entryline*, is the line along which the vertex is entered. If the vertex is active (statement 2) or there has been a previous even visit to it (statement 3), the routine returns. Otherwise, all edges incident with the vertex are checked by calling `oddvisit` (statement 7). If this call was successful, `entryline` is changed to non-

---

<sup>1</sup>FFMAXMAT stands for “flowerfree maximum matching”.

<b>FFMAXMATCH()</b>	
1	VERTEX <i>vtx</i> ;
2	forall (vertices <i>v</i> )
3	{ reset <i>vtattr</i> ; reset <i>vtactive</i> ;
4	if ( <i>v</i> is exposed && there are more than one exposed vertices left)
5	{ <i>vtx</i> = <b>evenvisit</b> ( <i>v</i> , NULL);
6	if ( <i>vtx</i> != NULL) mark <i>v</i> and <i>vtx</i> as covered;
7	else mark <i>v</i> as frustrated;
8	}
9	}

Table 4: Main loop of algorithm FFMAXMAT

matching line and the end vertex of the augmenting path is returned. If none of the calls were successful, the vertex is set inactive and NULL is returned.

**oddvisit:** Input parameters are a vertex  $v$  and an edge **entryline**. At first it is tested whether  $v$  is inactive and an odd visit is allowed, If so, the corresponding fields are set. Then it is checked if  $v$  is exposed. If it is, we have found an augmenting path. **entryline** becomes a matching line and  $v$  is returned as end point of the augmenting path. If  $v$  is not exposed it must be covered, for it cannot be frustrated. In this case there must exist a matching line incident with  $v$  and different from **entryline**. The routine **findmed** determines this edge. Along this edge **evenvisit** is called and the alternating depth-first search continued. Depending on the value returned, we know that an augmenting path has been found and its end vertex returned or that no augmenting path exists.

## 4.2 Correctness and Efficiency of the Algorithm

### 4.2.1 Correctness

**Theorem 4.1** *There is an augmenting path starting in exposed vertex  $v$  if and only if algorithm FFMAXMAT finds one.*

**Proof:** It is clear, that the algorithm will not find an augmenting path if there is none. Assume

$$v = v_0, v_1, v_2, \dots, v_i, v_{i+1}, \dots, v_n = u$$

is an augmenting path from exposed vertex  $v$  to exposed vertex  $u$ . This path determines an even/odd characteristic of all its vertices. We shall say that algorithm FFMAXMAT visits vertex  $v_i$  of the path *correctly* if the vertex is visited with its path-specific even/odd characteristic. The algorithm visits vertex  $v_0$  correctly. If it has visited vertex  $v_i$  correctly and the vertex is of odd visit then either  $v_i = v_n$  or the next visit is even and leads to  $v_{i+1}$ . If  $v_i$  is of even visit, the all its covered neighbors are checked. If no augmenting

```

VERTEX    *evenvisit(VERTEX *v, EDGE *entryline)

1  VERTEX    *vtend, *vtx;
2  if (v->vactive) return NULL;
3  if (v->vattr == E || v->vattr == EO) return NULL; // Previous even visit
4  v is set active;
5  update v->vattr to E or EO;
6  forall (edges ed incident with v and different from entryline)
7      { vtend = oddvisit(otherend(ed, v), ed);
8        if (vtend != NULL) // Augmenting path found
9            {if (entryline != NULL) change entryline to non-matching edge;
10           return vtend;
11          }
12      }
13  set v not active;
14  return NULL;

```

Table 5: Routine *evenvisit*

path is found beforehand  $v_{i+1}$  will be the next vertex visited correctly. Hence either an augmenting path is found beforehand or eventually  $v_n$  is found correctly and thus the initial augmenting path is found.  $\square$

#### 4.2.2 Efficiency

In each dfs run every edge is processed at most twice. So, the worst case complexity of the depth first search is  $O(m)$  where  $m$  is the number of edges. This is still true if changing edges to a new matching is added. In the worst case the dfs has to be run  $n$  times where  $n$  is the number of vertices. As a result we have  $O(nm)$  as the worst case complexity of the new algorithm.

### 4.3 Concluding Remarks

**General Graphs.** The preceding definitions and proofs are formulated for undirected graphs without loops and multiple lines. However, as can easily be seen, everything works as well if general graphs are used. The modified alternating depth-first search has to be an a-depth-first search.

**Initial Matching.** As with other matching finding algorithms, it will be useful not to start FFMAXMAT with an empty matching. We should start with a matching as large as possible, for instance with a saturated matching found by a greedy algorithm. Then, the lines of that matching have to be marked as such in the beginning. In addition, their incidence points have to be marked as covered.

```

VERTEX    *oddvisit(VERTEX *v, EDGE *entryline)

1  VERTEX    *vtend, *vtx;
2  EDGE      *med;
3  if (v->vactive) return NULL;
4  if (v->vtattr == O || v->vtattr == EO) return NULL; // Previous odd visit
5  set v active;
6  update v->vtattr to O or EO;
7  if (v is exposed) // augmenting path found
8    { change entryline to matching edge;
9      return v;
10   }
11 else
12   { med = findmed(v);
13     vtx = evenvisit(otherside(med, v), med);
14     if (vtx != NULL) // augmenting path found
15       { change entryline to matching edge;
16         return vtx;
17       }
18     set v not active;
19     return NULL;
20   }

```

Table 6: Routine *oddvisit*

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*Pages where cited are in parentheses.*

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